



H_3^+ in the Diffuse Interstellar Medium
The Problem of the Ionization

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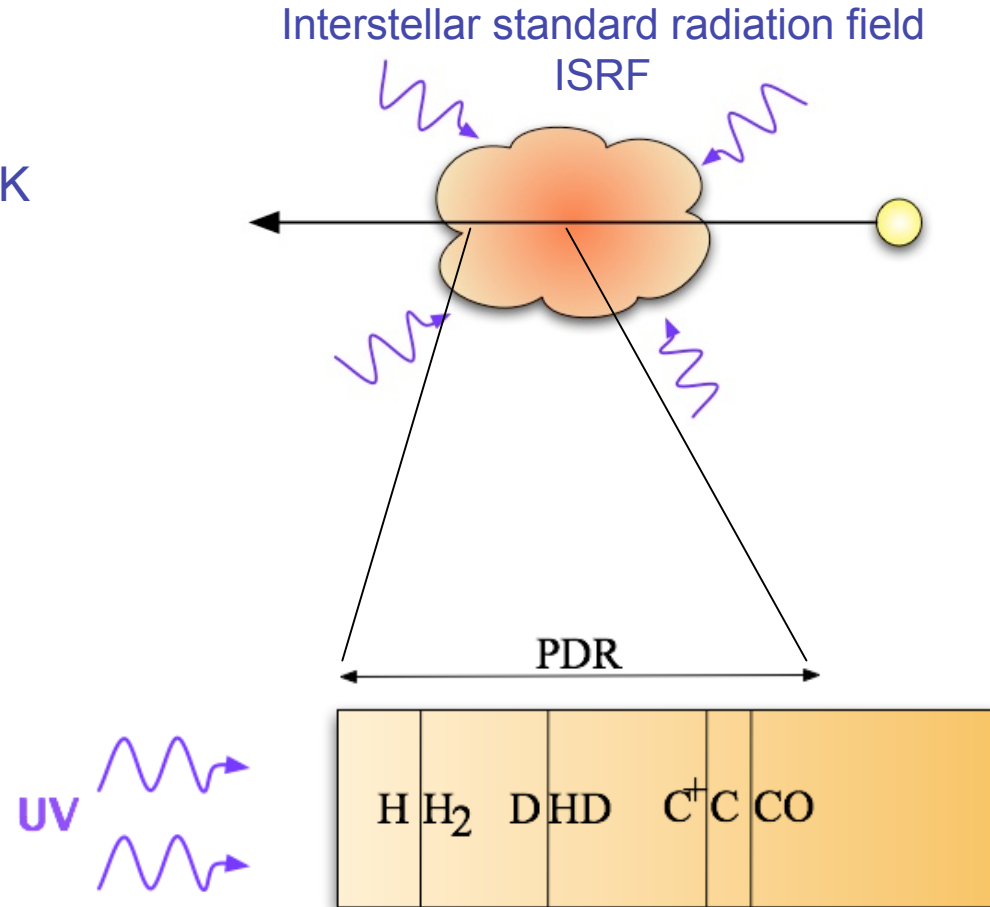
Diffuse clouds

Properties:

- Density: $n_{\text{H}} \approx 100 \text{ cm}^{-3}$
- embedded in the ISRF
- Kinetic temperature $T_{\text{kin}} \approx T_{01} \approx 70 \text{ K}$
- Transition between atomic and molecular hydrogen

Observation in absorption possible

- Far UV : H, H₂, HD, CO, ...
- Visible: OH, CH, CH⁺, CN,
C₂, C₃, ...
- IR: H₃⁺
- Radio : HCO⁺, HOC⁺, NH₃,
HCN, HNC, H₂S, ...



Interest to study diffuse clouds

Simple chemistry → good place to understand the physics of ISM

Two fundamental questions:

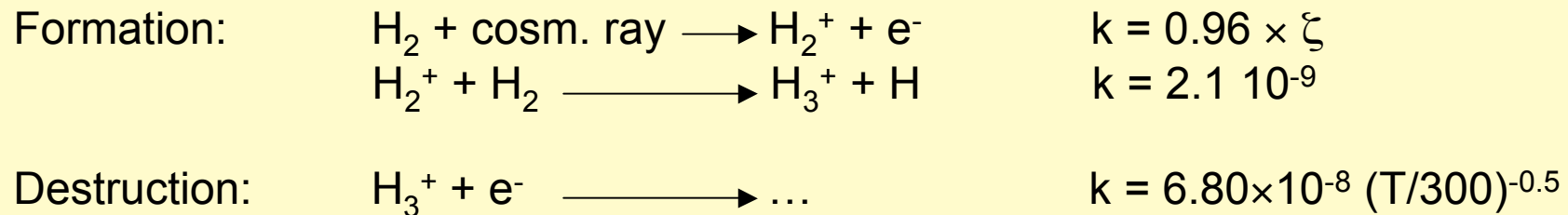
- **dissipation of energy**

- formation process of CH^+
- rotational excitation of H_2

- **ionization**

- the formation of many molecules is initiated by cosmic rays ionization

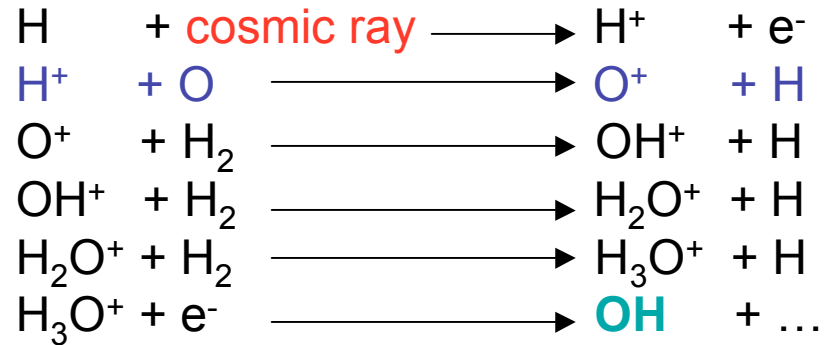
H_3^+ , HD, OH, ...



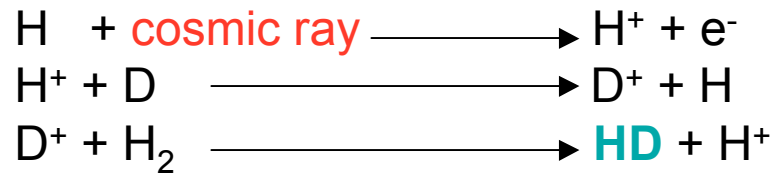
$$n(\text{HD}), n(\text{OH}), n(\text{H}_3^+) \propto \zeta$$

Determination of the ionization rate by cosmic rays

(Black et Dalgarno 1973, Black et al. 1978, Federman et al. 1996, Le Petit et al. 2001)



$n(\text{OH}) \propto \text{cosmic rays flux}$

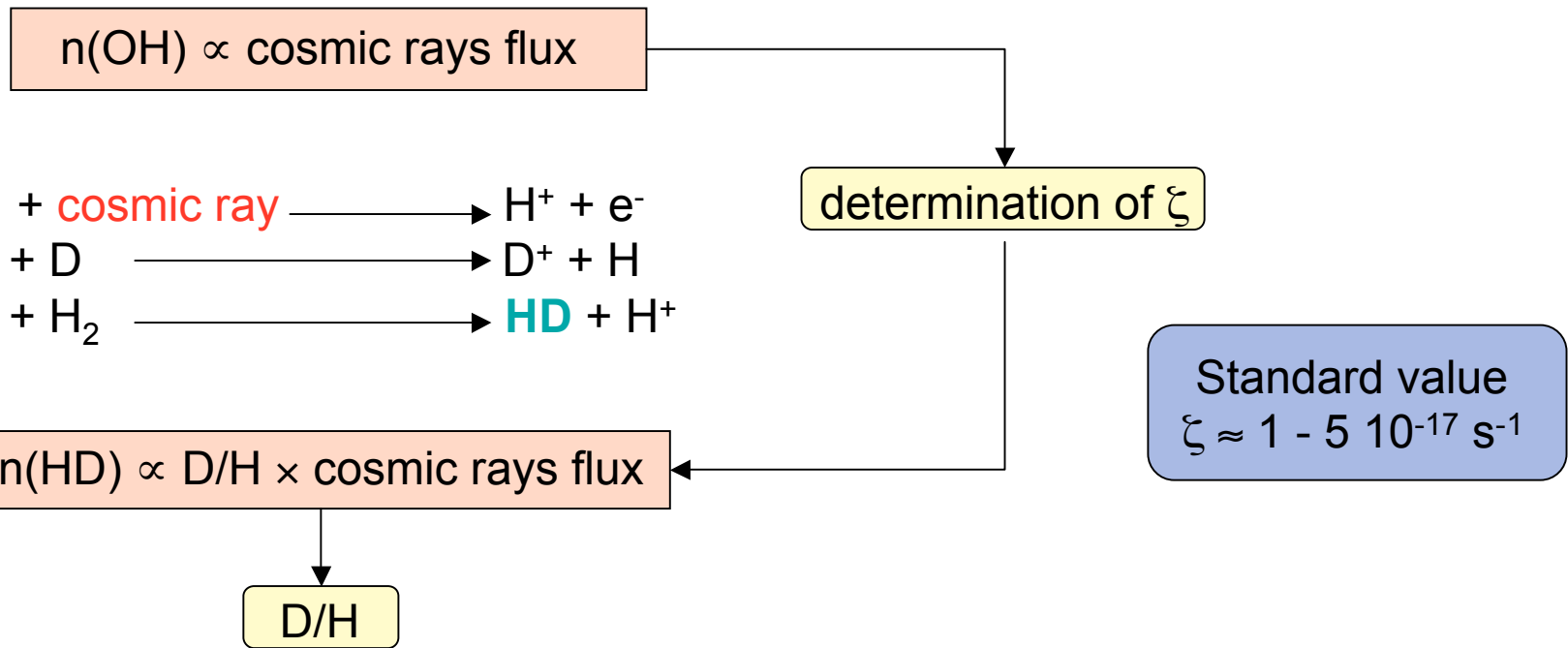


$n(\text{HD}) \propto \text{D/H} \times \text{cosmic rays flux}$

D/H

determination of ζ

Standard value
 $\zeta \approx 1 - 5 \cdot 10^{-17} \text{ s}^{-1}$



H₃⁺ in diffuse clouds

Observation:

- detected on 8 diffuse lines of sight
 $N(\text{H}_3^+) / E(\text{B-V}) \sim \text{some } 10^{14}$
 $\Rightarrow 10 \times$ higher than dense clouds

- in diffuse medium near the Galactic center
(Oka et al. 2005)

Model: $n_{\text{H}} = 100 \text{ cm}^{-3}$
 $\chi = 1$
 $T = 60 \text{ K}$
 $\zeta = 5 \times 10^{17} \text{ s}^{-1}$
 $N_{\text{H}} = 10^{21} \text{ cm}^{-2}$



$$N(\text{H}_3^+) = 8 \times 10^{12} \text{ cm}^{-2}$$

	E(B-V)	N(H ₃ ⁺)
Cyg. OB2 12	3.35	2.02 (14)
Cyg. OB2 5	1.99	~ 3 (14)
HD 183143	1.28	~ 2 (14)
HD 20041	0.70	1.74 (14)
WR 104	2.10	~ 2 (14)
WR 118	4.13	~ 4 (14)
WR 121	1.68	1.12 (14)
ζ Per	0.32	8.0 (13)
Gal. center		3.1 (15)

Ref: McCall et al. (2002)
 McCall et al. (2003)
 Oka et al. (2005)

The Zeta Per line of sight

A very well studied line of sight

Spectral type : B1

$R_V = 2.8$ (Cardelli et al. 1989)

$E(B-V) = 0.32$ (van Dishoeck & Black 1989)

A very good test for models

	Observation
H ₂	3.2 - 7.1 (20)
H ₂ (J=0)	2.2 - 4.8 (20)
H ₂ (J=1)	1.0 - 2.3 (20)
H ₂ (J=2)	1.1 - 2.4 (18)
H ₂ (J=3)	2.0 - 9.6 (16)
H ₂ (J=4)	1.1 - 2.0 (15)
H ₂ (J=5)	2.3 - 2.8 (14)

	Observations	
H	5.7(20)	7.1(20)
H ₂	3.2(20)	7.1(20)
f	0.53	0.66
T ₀₁	45	75
HD	2.0(15)	1.1(16)
H ₃ ⁺	8.0(13)	
C ⁺	1.8(17)	
C	2.9(15)	3.6(15)
CO	5.4(14)	
CH	1.9(13)	2.0(13)
CH ⁺	3.5(12)	
C ₂	1.6(13)	2.2(13)
C ₃	1.0(12)	
CN	2.7(12)	3.3(12)
NH	9.0(11)	
O	0.2(18)	1.0(18)
OH	4.0(13)	
S ⁺	1.7(16)	2.3(16)
S	1.5(13)	2.2(13)
Si ⁺	2.8(16)	2.8(14)

Determination of the flux of cosmic rays

- Black, Hartquist & Dalgarno (1978)
 - 2 components model
 - cold zone: $T = 45 \text{ K}$, $n_{\text{H}} = 267 \text{ cm}^{-3}$
 - hot zone: $T = 120 \text{ K}$, $n_{\text{H}} = 100 \text{ cm}^{-3}$

$$\zeta = 2.2 \times 10^{-17} \text{ s}^{-1}$$

- van Dishoeck & Black (1986)
 - all constraints taken into account (at this time ...)
 - models with T and n_{H} profile

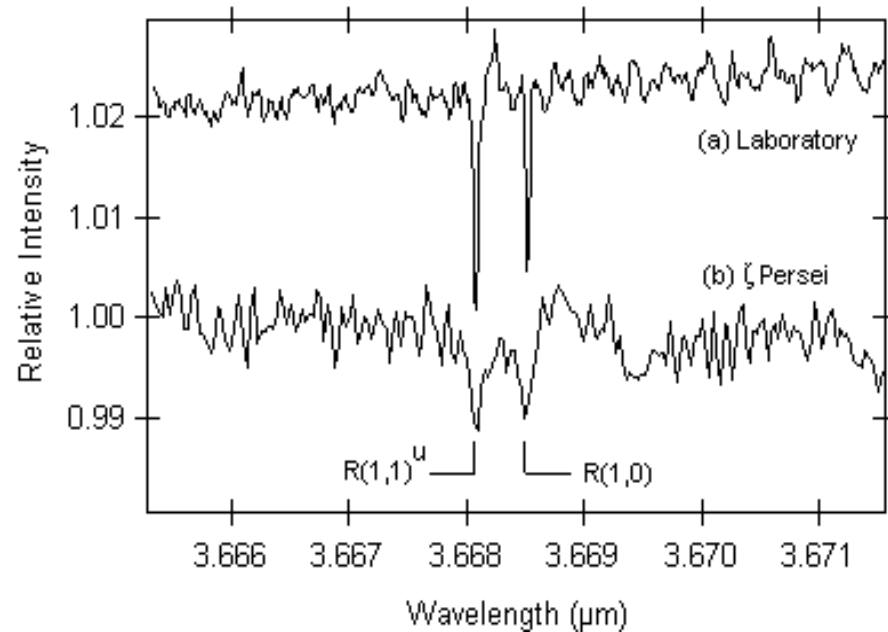
$$\zeta = 4-7 \times 10^{-17} \text{ s}^{-1}$$

- Federman et al. (1996)
 - From OH only : $\zeta = 1.7 \times 10^{-17} \text{ s}^{-1}$

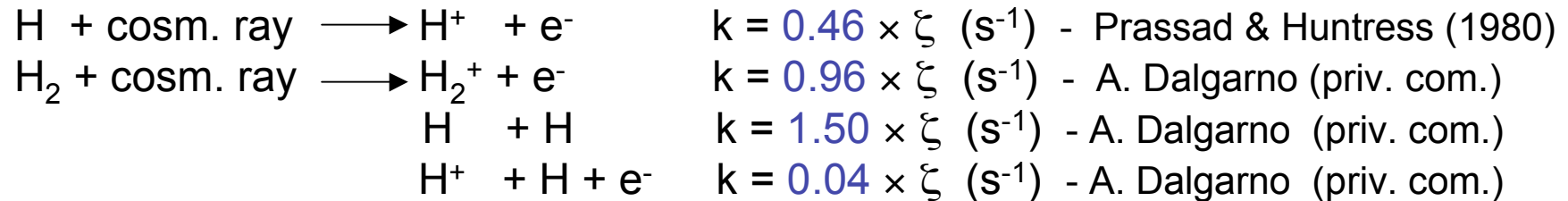
Observation of H_3^+ towards ζ Per:

- McCall et al. (2003) :
 - Determination of the recombination rate of H_3^+
 - $N(H_3^+) = 8.0 \times 10^{13} \text{ cm}^{-2}$

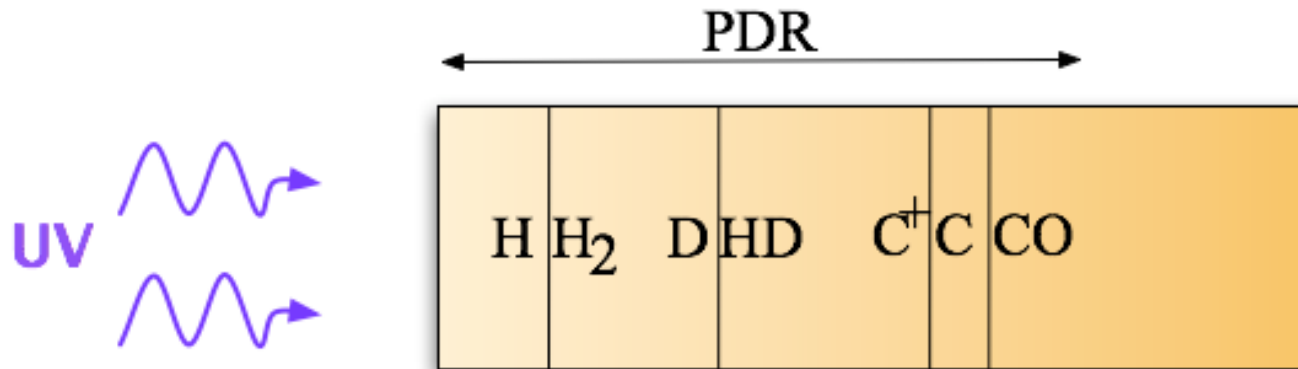
$$\zeta = 1.2 \times 10^{-15} \text{ s}^{-1}$$



Comparison of ζ between different authors not always simple:



The Meudon PDR code (<http://aristote.obspm.fr/MIS>)



Stationary model solving:

- **Radiative transfer:** absorption in the lines of H, H₂, CO, HD, ...
absorption in the continuum
- **Chemistry:** more than 100 chemical species
network of more than 1000 chemical reactions
photoionization
- **Statistical equilibrium of the populations in the levels of H₂, HD, CO, HCO⁺, CS, ...**
takes into account: radiative and collisional excitation / de-excitations
photodissociation
- **Thermal balance:** heating by photoelectric effect, chemistry, cosmic rays ...
cooling in the lines of atoms and molecules

Modelisation of the ζ Per line of sight

(Franck Le Petit, Evelyne Roueff & Eric Herbst, A&A, 2004)

Parameters and hypothesis :

$$R_V = 2.8$$

Isothermal model : $T_{01} = 60 \text{ K}$ (45-75 K)

$$N(\text{H}_2) = 4.5 \times 10^{20} \text{ cm}^{-2}$$

$$n_{\text{H}} = 100 \text{ cm}^{-3}$$

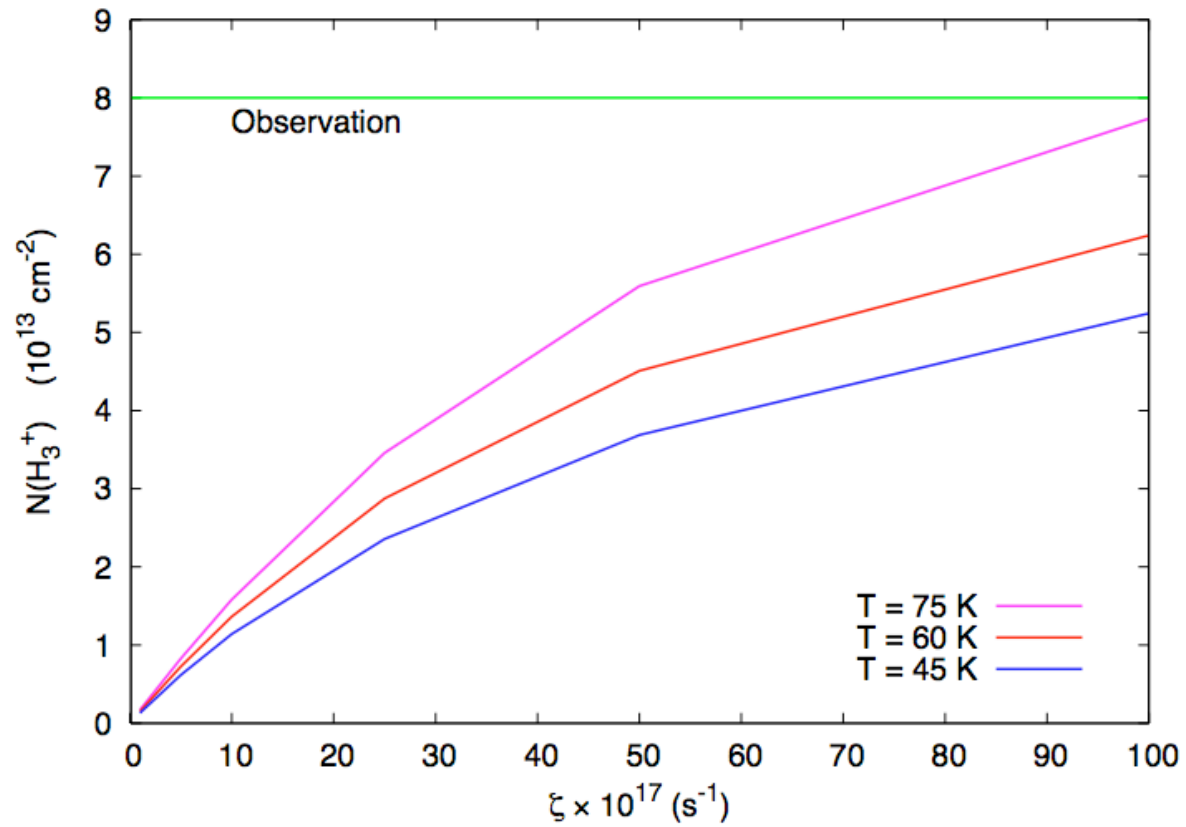
$$\chi = 2$$

	Relative abundance
D/H	1.5 (-5)
O/H	3.2 (-4)
N/H	7.5 (-5)
C/H	1.32 (-4)
S/H	1.86 (-5)
Si/H	2.9 (-5)

Variation of ζ between 1×10^{-17} and $100 \times 10^{-17} \text{ s}^{-1}$

↪ effect on species sensible to ζ

Determination of ζ from H_3^+



Depends on T

Observations require : $\zeta \sim 100 \times 10^{-17} \text{ cm}^{-3}$

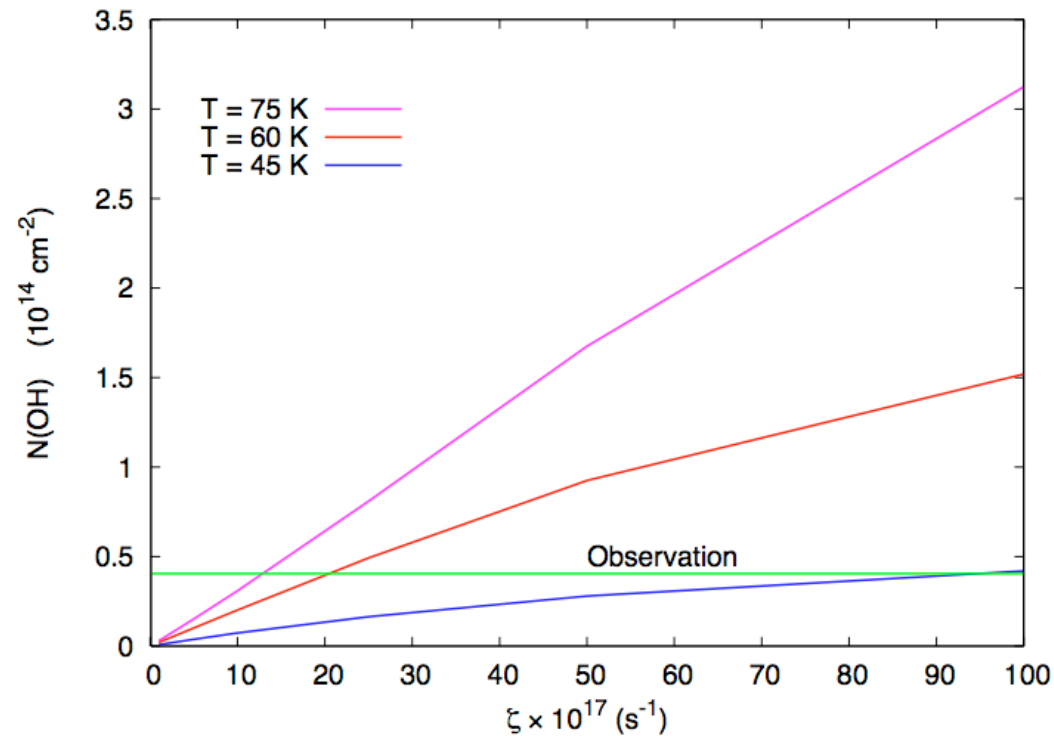
Determination of ζ from OH

$n(\text{OH})$ is highly dependent on T



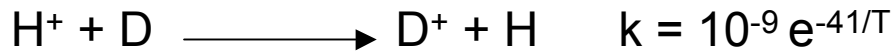
$$45 \text{ K} \quad k = 3.9 \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}$$

$$75 \text{ K} \quad k = 2.9 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$$



HD as a constraint on ζ

- not much dependent on T

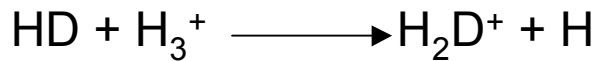


- good constraint for $\zeta < 10^{-16} \text{ s}^{-1}$

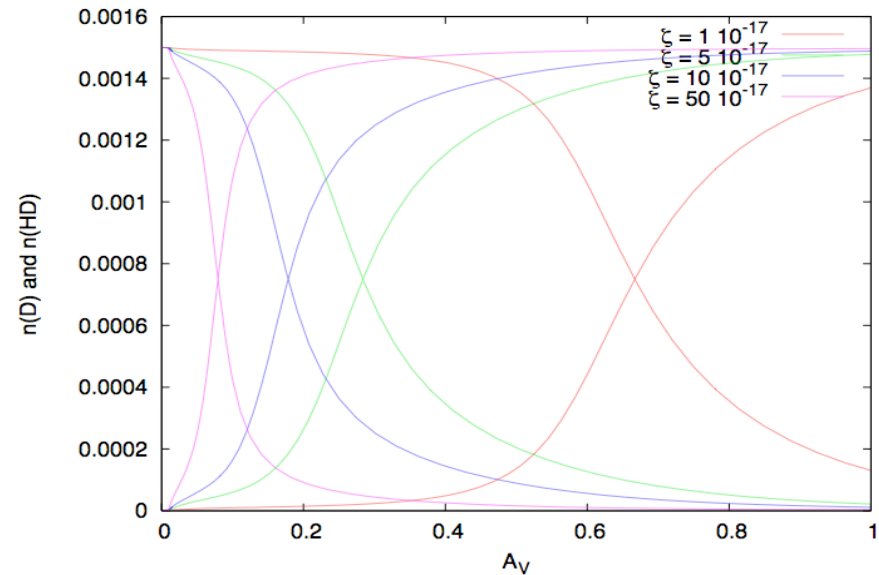
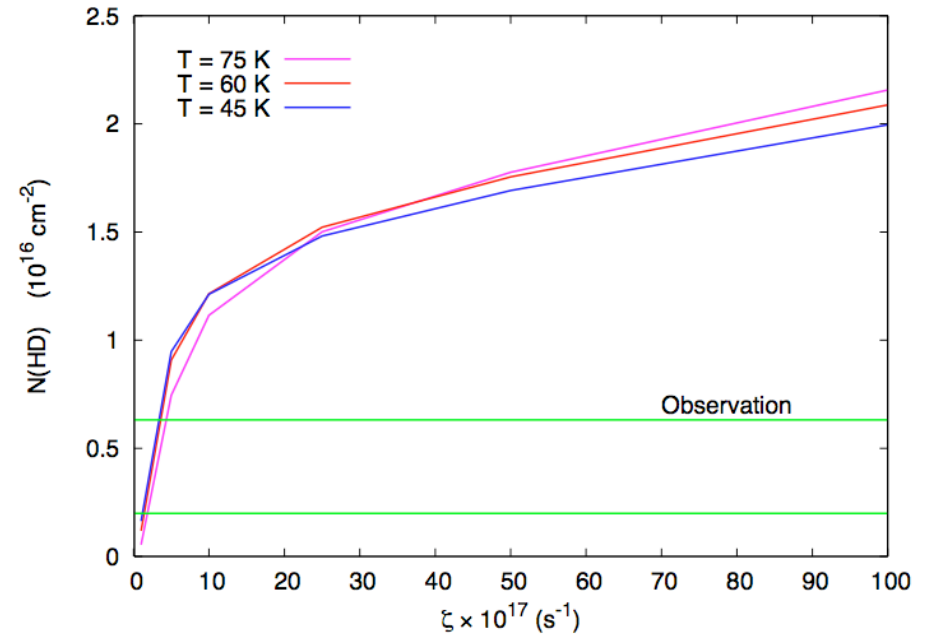
$n(\text{HD}) \propto \zeta$ if:

- 1) It is formed in gas phase by $\text{D}^+ + \text{H}_2$
- 2) It is destroyed by photodissociation

after the D/HD transition :



$n(\text{HD})$ no more proportionnal to ζ



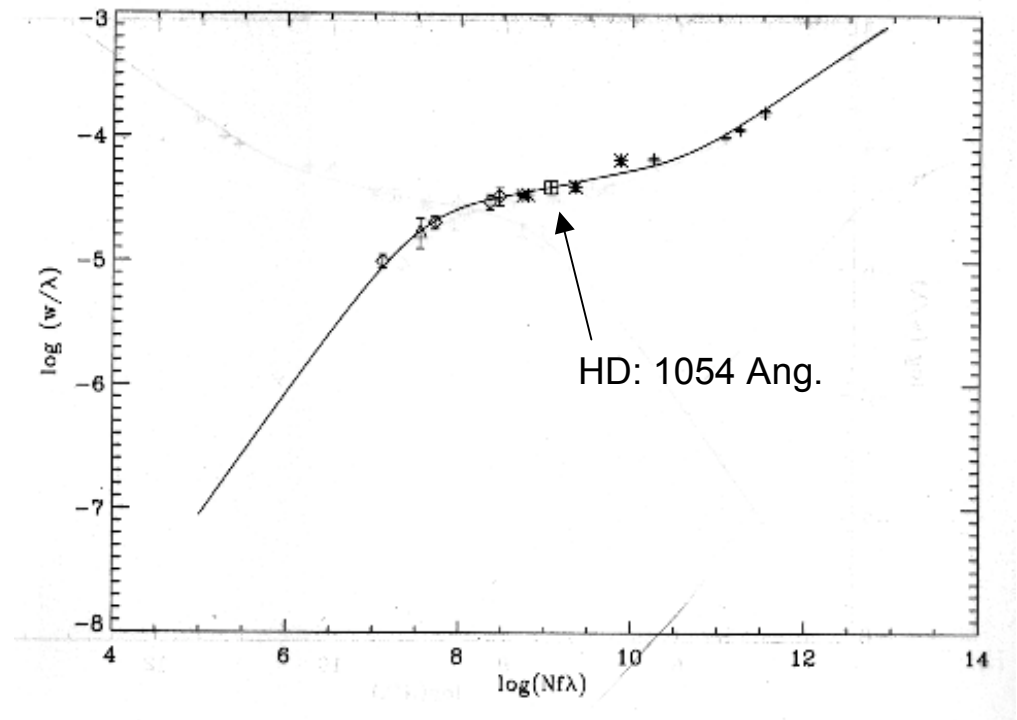
- still some debates on D/H
- difficult to get a precise value of N(HD)

Determination of N(HD) requires to know precisely the b Doppler parameter

Towards ζ Per :

- Only HD at 1054 Ang. detected
- flat part of the curve of growth
- Re-analysis with updated H_2 , f values (Abgrall et al. 1993)
 - max value: $1.1 \times 10^{16} \text{ cm}^{-2}$
 - instead of $5.1 \times 10^{15} \text{ cm}^{-2}$ (Snow 1977)

Other lines of sight: same problem



Conclusion from N(HD) :

$\xi > 5 \cdot 10^{-17} \text{ s}^{-1}$ overestimates slightly N(HD)

(with D/H = $1.5 \cdot 10^{-5}$)

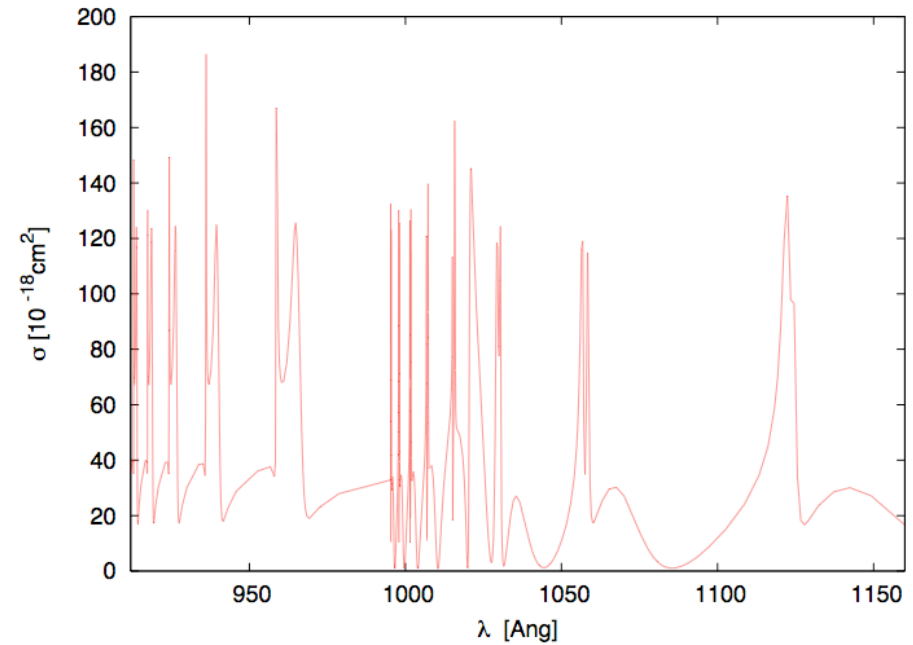
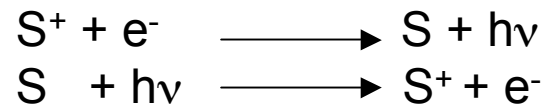
The neutral and ionized atoms

High ζ increases the ionization degree

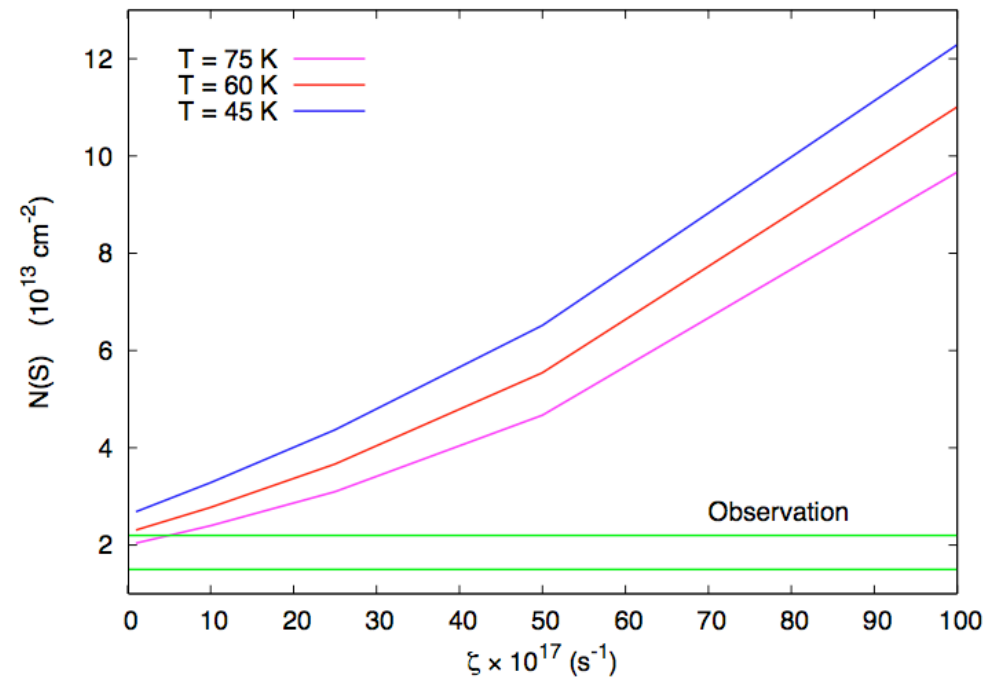
Efficient recombination with electrons :

S^+ does not react with H or H_2

↪ reactive recombination dominates



$\zeta = 100 \times 10^{-17} \text{ s}^{-1}$
↓
overproduction of neutral sulfur



Conclusion about the ζ Per line of sight

$n_{\text{H}} = 100 \text{ cm}^{-3}, \chi = 2$ $T = 60 \text{ K},$ $N(\text{H}_2) = 4.5 \cdot 10^{20} \text{ cm}^{-2}$
--

ζ [10^{-17} s^{-1}]	H_3^+ [cm^{-2}]	OH [cm^{-2}]	HD [cm^{-2}]	S [cm^{-2}]
1	1.5 (12)	1.6 (12)	1.7 (15)	1.7 (13)
25	3.0 (13)	4.1 (13)	1.5 (16)	2.6 (13)
100	6.3 (13)	1.4 (14)	2.0 (16)	8.2 (13)
Obs.	8.0 (14)	4.0 (13)	2.0 (15) 1.1 (16)	1.5 (13) 2.2 (13)

- **Standard value of ζ**
Underestimate $N(\text{H}_3^+)$
by a factor 50

- **$\zeta = 100$ times the standard value and $T = 60 \text{ K}$**

Reproduce $N(\text{H}_3^+)$ but overproduce
OH by a factor 4
S by a factor 6

T can be decreased to 45 K to match better OH
negative impact on C, S, H_3^+

χ can be increased to match better S
molecules too much photodissociated

- **$\zeta = 25 \times 10^{-17} \text{ s}^{-1}$ good compromise to fit all abundances**

H₃⁺ towards the Galactic center

Observations (*Oka et al. 2005*)

Clouds	N(H ₃ ⁺) [10 ¹⁴ cm ⁻²]					HM	Total	T [K]	n [cm ⁻³]
	(1,1)	(3,3)	(2,2)	(1,0)					
-100 km s⁻¹	7.0±0.8	4.4 ± 0.9	≤ 0.7	2.9 ± 1.0	1.4 ± 0.7	15.7 ± 1.7	270 ± 70	≤ 50	
-50 km s ⁻¹	2.6 ± 0.5	1.6 ± 0.6	0.4 ± 0.4	1.6 ± 0.9	0.4 ± 0.2	6.6 ± 1.3	250 ± 100	≤ 100	
0 km s ⁻¹	4.9 ± 0.5	1.0 ± 0.7	≤ 0.7	2.4 ± 1.3	0.1 ± 0.1	8.4 ± 1.6	130 ± 100	≤ 200	

Constraints : Populations \longleftrightarrow n_{H}, T : Parameters
 $N(\text{H}_3^+)$ \longleftrightarrow $\zeta, L, (\chi)$
 $N(\text{CO}, J=0) < 3 \cdot 10^{16}$
 $f = 0.5 - 1$

H₃⁺ excitation

- Oka & Epp (2004) prescription for collision rates:

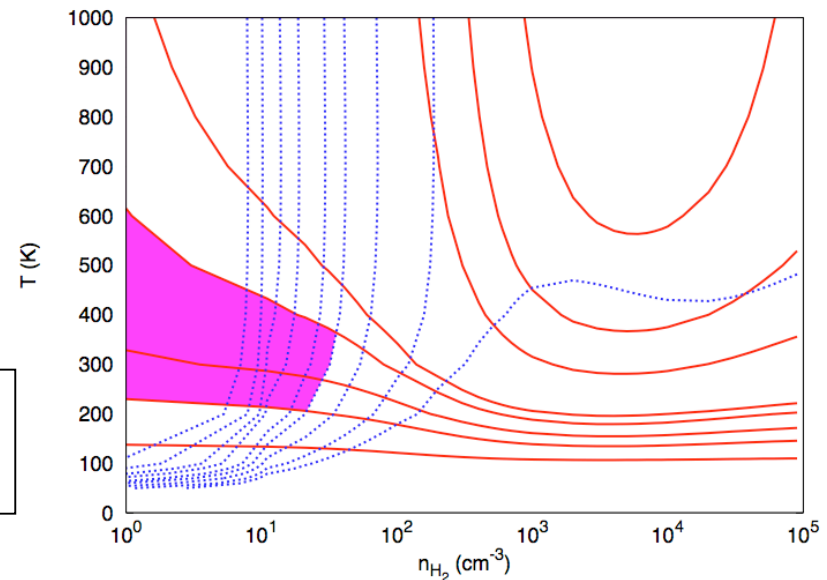
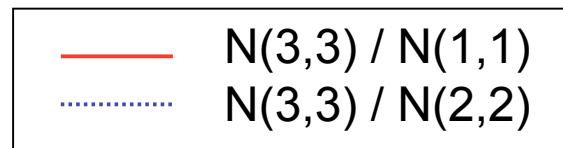
$$k_{JK}^{J'K'} = C_{JK}^{J'K'} \sqrt{\frac{g_{JK}}{g_{J'K'}}} \exp\left(-\frac{E_{JK} - E_{J'K'}}{2kT}\right)$$

$$C_{JK}^{J'K'} = C_{J'K'}^{JK} = C \left\{ 1 + \sum_{J''K''} \left(\frac{g_{J''K''}}{\sqrt{g_{JK}g_{J'K'}}} \right)^{1/2} \exp\left[-\frac{E_{J''K''} - (1/2)(E_{JK} + E_{J'K'})}{2kT}\right] \right\}^{-1}$$

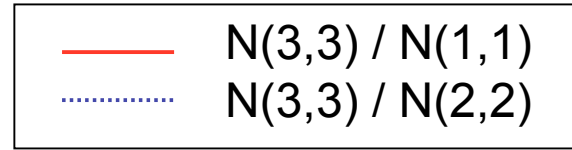
C = 2×10⁻⁹ cm³ s⁻¹ : Langevin rate constant for H₃⁺ + H₂

- Einstein coefficients from Lindsay & McCall (2001)

Small program to compute H₃⁺ excitation
 ↪ same results than Oka & Epp (2004)

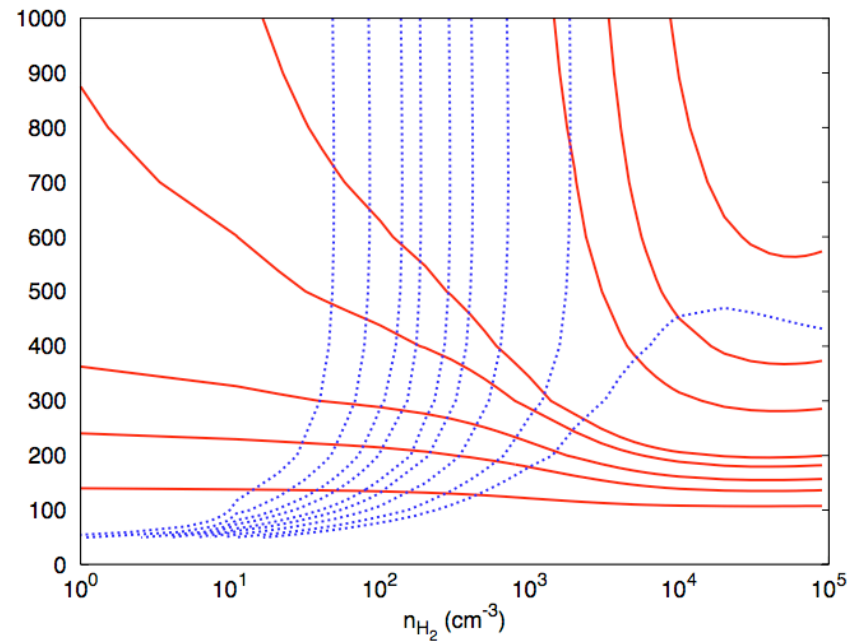
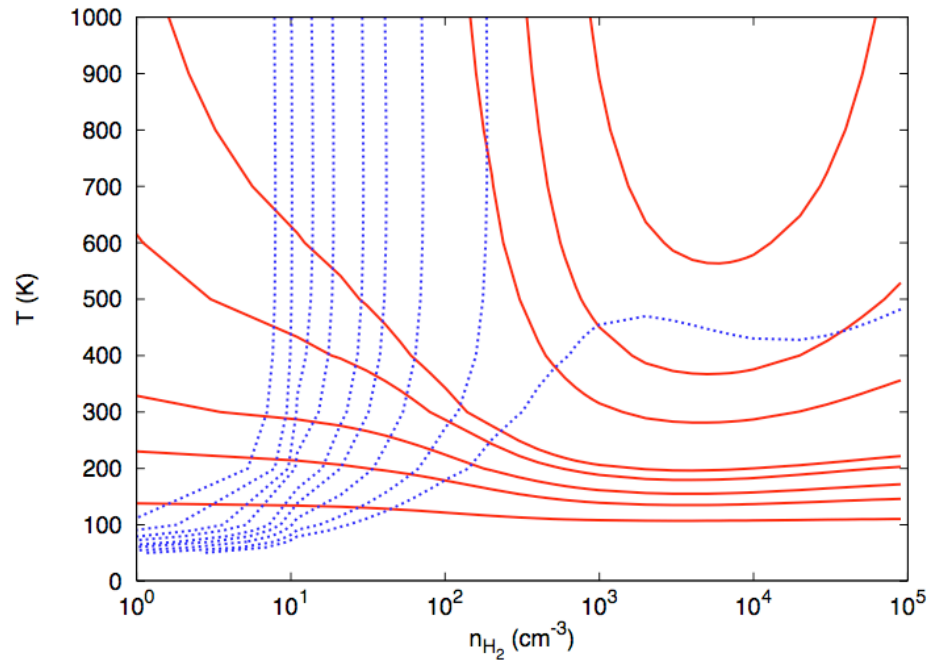


Variation of the collision rates



$$C_{\text{Langevin}} = 2 \cdot 10^{-9}$$

$$C_{\text{Langevin}} = 2 \cdot 10^{-10}$$



Reduction of C_{Langevin} :

n-T domain reproducing the observations increases higher densities & temperatures allowed

New implementations in the PDR code

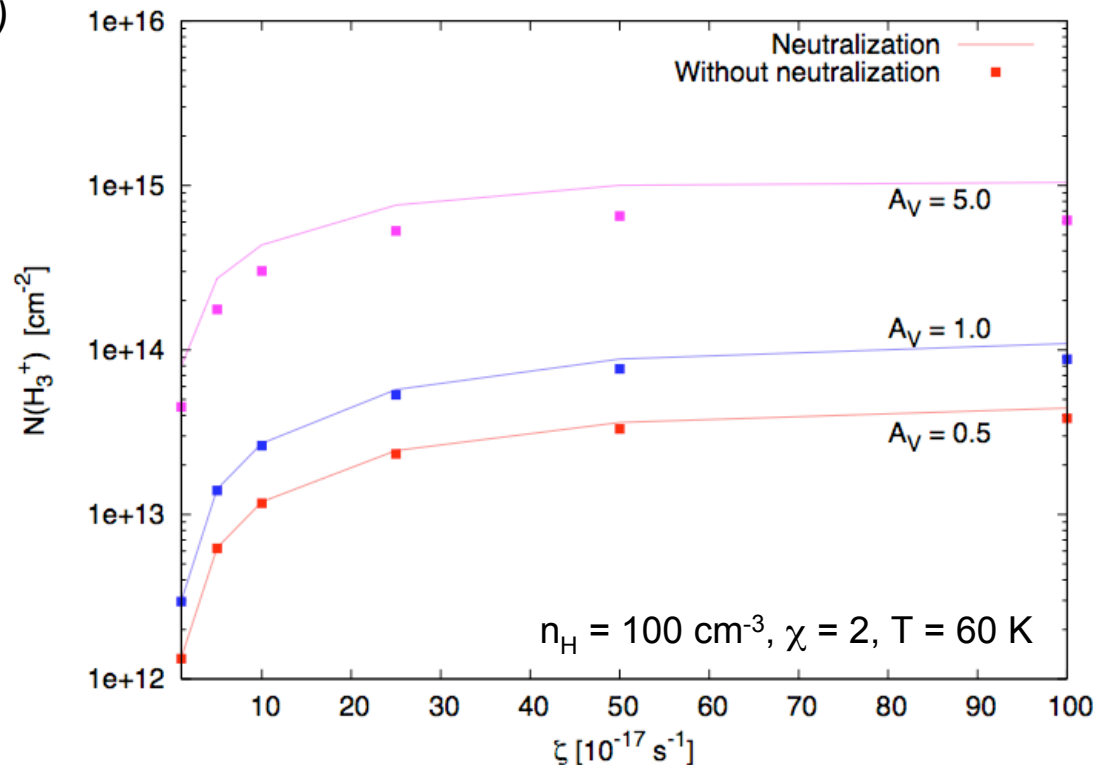
1. Statistical balance of H_3^+

- H_3^+ formed following a Boltzman distribution at T_{kin}
 - Tests: formation in specific levels
 - ↪ no significant differences
- destruction independent of levels

2. Neutralization of atomic ions on grains

(Previous study by H. Liszt 2003)

$\zeta = 100$ $\times 10^{-17} \text{ s}^{-1}$	$N(H_3^+)$	
	With neutr.	Without neutr.
$A_V = 0.5$	4.4 (13)	3.8 (13)
$A_V = 1.0$	1.1 (14)	8.8 (13)
$A_V = 5.0$	1.0 (15)	6.1 (14)



Isothermal PDR models

$$\chi = 10, \quad R_X = 3$$

n [cm ⁻³]	ξ [10 ⁻¹⁷ s ⁻¹]	T [K]	L [pc]	f	N(CO) [cm ⁻²]	J = 1 [cm ⁻²]	N(H ₃ ⁺) [cm ⁻²]	1,1 [cm ⁻²]	2,2 [cm ⁻²]	3,3 [cm ⁻²]
10	25	270	100	0.61	1.3 (17)	6.6 (16)	1.2 (15)	5.2 (14)	1.2 (13)	3.0 (14)
	50	270	100	0.42	1.4 (17)	7.0 (16)	1.2 (15)	5.4 (14)	1.4 (13)	3.2 (14)
	100	270	100	0.23	4.4 (16)	1.7 (16)	5.7 (14)	2.5 (14)	7.4 (12)	1.5 (14)
50	50	270	20	0.82	1.5 (17)	6.6 (16)	8.7 (14)	3.5 (14)	3.3 (13)	2.3 (14)
		270	31	0.83	3.4 (17)	1.3 (17)	1.8 (15)	7.3 (14)	6.9(13)	4.8(14)
		200	31	0.83	3.9 (17)	1.5 (17)	1.6 (15)	7.0 (14)	6.0 (13)	3.1 (14)
		150	33	0.84	4.7 (17)	1.7 (17)	1.5 (15)	7.0 (14)	5.4 (13)	1.9 (14)
	100	270	22	0.70	2.4 (17)	1.0 (17)	1.7 (15)	6.7 (14)	6.9 (13)	4.5 (14)
	500	270	31	0.26	1.7 (17)	8.2 (16)	1.5 (15)	5.5 (14)	7.5 (13)	3.8 (13)
Observations		min max	15-20	0.5 1		< 3 (16)	1.4 (15) 1.7 (15)	6.2 (14) 7.8 (14)	< 7 (13)	3.5 (14) 5.3 (14)

Thermal Balance

How to have $N(\text{H}_3) = 10^{14} \text{ cm}^{-2}$ in a diffuse medium ($n_{\text{H}} < 50 \text{ cm}^{-3}$) at 270 K ?

Galactic center :

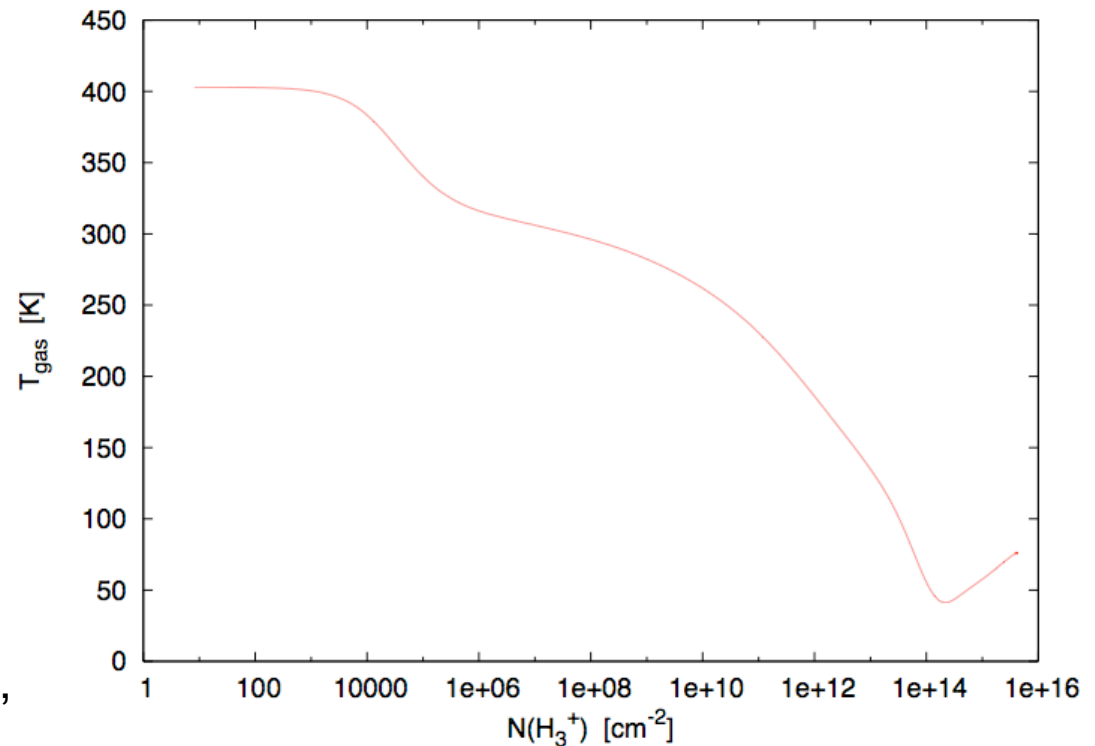
Radiation field higher

$R_{\text{X}} = 3 - 10 \Rightarrow$ more coolants

X-Rays and cosmic rays
shocks & turbulence

$\rightarrow 5-40 \text{ km s}^{-1}$

(Rodriguez-Fernandez et al. 2004)



Model with thermal balance :

Medium : $n_{\text{H}} = 50 \text{ cm}^{-3}$, $R_{\text{X}} = 3$,

Photoelectric effect : $\chi = 10$

$r_{\text{min}} = 1 \text{ nm}$

Cosmic ray heating : $\zeta = 100 \times 10^{-17} \text{ s}^{-1}$

Energy input by cosmic ray: $\gamma = 4 - 6 \text{ eV}$

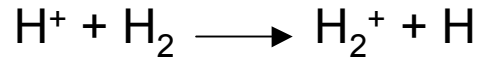
Turbulence : Shocks & Vortex

1 - C-shock model :

Pre-shock density : 20 cm^{-3}

$V_{\text{shock}} = 50 \text{ km s}^{-1}$

$B = 7 \text{ mG}$



$$k = 6.4 \times 10^{-10} e^{-21300/T}$$

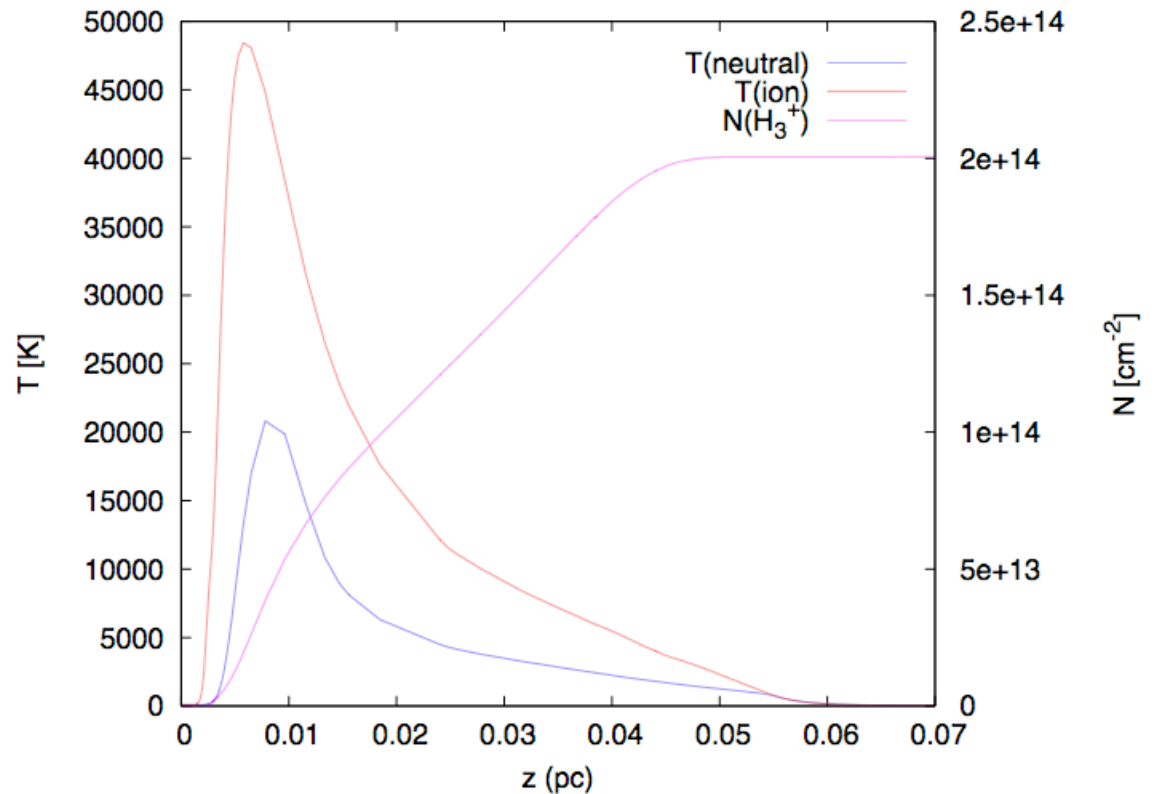
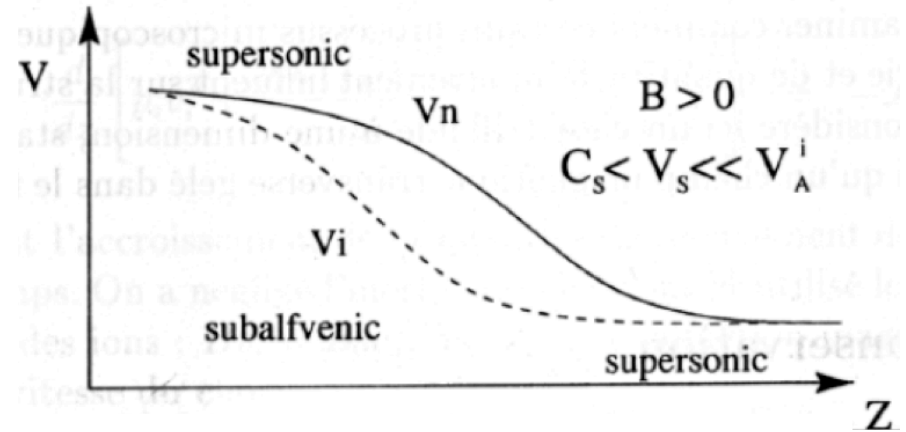
$N(\text{H}_3^+) = 2.0 \times 10^{14} \text{ cm}^{-2}$
 $N(\text{CH}^+) = 9.1 \times 10^{13} \text{ cm}^{-2}$
 $N(\text{CO}) = 5.0 \times 10^{13} \text{ cm}^{-2}$

Best PDR isothermal model

$$N(\text{H}_3^+) = 1.7 \times 10^{15} \text{ cm}^{-2}$$

$$N(\text{CH}^+) = 1.1 \times 10^{12} \text{ cm}^{-2}$$

$$N(\text{CO}) = 2.4 \times 10^{17} \text{ cm}^{-2}$$



2 - Vortex

Local and temporal heating of the gas allowing to overcome activation thresholds

- Introduced by K. Joulain & E. Falgarone (1998)

↳ formation of CH⁺



- Cecchi-Pestelini, Casu, Dalgarno (2005)

Model of vortex to compute H₂ excitation

↳ Reproduce rotationnal H₂ excitation (J > 2) in standard diffuse medium

=> test this on the H₃⁺ excitation